FPP: AN AUTOMATIC PROGRAM PROVER FOR ADA STATEMENTS

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Abstract
The Frege Program Prover (FPP) is an experimental system which supports the programmer when calculating the effect or semantics of programs or program fragments formulated in the Ada language. FPP supports two kinds of such calculations:

a) Compute the weakest precondition: wp(PF, Post): compute the weakest precondition for a given program (fragment) PF and a given postcondition Post.

b) Check the correctness of a program (fragment): i.e. check whether a given program (fragment) PF satisfies a given specification (Pre,Post). This is usually expressed as a Hoare triple {Pre} PF {Post}. If PF satisfies the specification the triple is called consistent. This consistency is defined as: [Pre⇒wp(PF,Post)].

The assertions (precondition, postcondition, loop invariant etc.) are written as special comments (e.g. --!pre: .... ). This means that an annotated program is still a legal Ada program.

FPP is an example of an automatic program prover (APP), i.e. the proofs are done in a purely mechanical fashion without any intervention by the user. The user gives an annotated program as input and gets as output the result.

FPP is implemented as a WWW application (http://www1.informatik.uni-jena.de/FPP/FPP-main.htm) and supports a subset of Ada: Integer and Boolean variables, assignment, sequence, IF, CASE, FOR, and WHILE.

1 Introduction
Software has become an important and often essential part of technical systems. It is used in small devices as e.g. pacemakers up to big systems as e.g. airplanes. Both are examples of systems which require a high degree of reliability and safety. This means that all parts of design must be checked whether they guarantee these requirements. For electrical or mechanical designs there exist methods to check properties in an exact manner: e.g. circuit analysis [Dor 93] or analysis of structure. Such methods are routinely applied by electrical or civil engineers.

In SW engineering such methods also exist but are not as mature as those in other fields of engineering and are therefore neither taught nor used routinely during the development of programs. Whereas any electrical engineer can perform the calculations necessary for the quantitative analysis of simple circuits it is usually not he case that a software engineer can calculate the effect of a simple program or program fragment in a quantitative way.

One important reason for this is the very rapid development of the field.

The Frege Program Prover (FPP) is an experimental system to support the SW engineer in such calculations.

FPP is implemented as a WWW application (http://www1.informatik.uni-jena.de/FPP/FPP-main.htm) and supports a subset of Ada: Integer and Boolean variables, assignment, sequence, IF, CASE, FOR, and WHILE.

2 Semantics or the Effect of Programs
As Dijkstra has pointed out it is the task of computers to execute the programs constructed by the SW engineers. The purpose of program execution is to put the computer in some specific state. Such a required final state can e.g. be a state in which a certain variable contains the sum of some other variables. In programs running continuously, as e.g. in embedded systems, this characterization holds for each cycle. The effect of a program can therefore be characterized by the relation between the initial state (in which it is started) and the final state(s) (in which it terminates). This is often also called the semantics of the program. In this paper we use mostly the term “effect”.

The most abstract description of the effect of a program is the relation between initial and final states [Win 96]. Usually programs are constructed out of smaller pieces (as e.g. modules, routines, declarations, statements). In order to compute the effect of the whole program two things must be known: (1) the effect of the smaller pieces and (2) how to compute the effect of a composition.

Example: if we know the effect of the two assignments “abs := x;” and “abs := -x;” we have to be able to compute the effect of:

\[
\text{IF } \min < x < 0 \\
\text{THEN } \text{abs := } -x; \\
\text{ELSE } \text{abs := } x; \quad \text{FI}
\]

The program state is therefore the basic entity for the characterization of the effect of programs. The program state is characterized by the values of all objects in the program. Especially important among these objects are the variables. In this paper we will characterize the program state by the values of the variables in the program [Win 96]:

**DEF-1:** \( V = \{ v_1, v_2, \ldots, v_n \} \) is the set of program variables, where \( n \geq 1 \).

\( W_1, W_2, \ldots, W_n \) are nonempty, finite sets of admissible values for the corresponding \( v_i \): \( W_i = \text{VS}(v_i) \).

\( W = W_1 \cup W_2 \cup \ldots \cup W_n \).

\( S = \{ s \in V \rightarrow W : (\forall v \in V: s(v) \in \text{VS}(v)) \} \) is the set of proper states, where \( V \rightarrow W \) denotes the set of functions from \( V \) into \( W \).

\( S_\bot = S \cup \{ \bot \} \) is the set of states.

\( C = 2^S \) is the set of proper conditions.

\( C_\bot = 2^{S_\bot} \) is the set of conditions.

**DEF-2:** \( \text{PROG} = \{ P \subseteq S \times S_\bot : \text{dom}(P) = S \} \) is the set of abstract programs.

An element \((i,f) \in S \times S_\bot\) is called a computation with initial state \( i \) and final state \( f \).

If \( f \neq \bot \) then we say the computation \((i,f)\) terminates properly; if \( f = \bot \) then the computation is a not(properly terminating) one. This behavior can occur in different forms: e.g. infinite loop or stop in the “middle” of the computation; therefore the somewhat unconventional expression “not(properly terminating)”.

In order to see how these abstract definitions work for programs we look at some examples.

**Exmp 1:** the effect of the assignment \( x:= 10 \); can be characterized as follows:

\( \{ 10 \in \text{VS}(x) \} \ x := 10; \{ x = 10 \} \).

This triple “condition statement condition” is a proposition which states: whenever the initial state is such that “10 \( \in \text{VS}(x) \)” holds then \( x:=10; \) is executable in this state and after termination the program is in a state in which \( x=10 \) holds. The precondition, in this case, is very simple: it is either true or false. If it is true it denotes the set \( S \) of all proper program states: \( \{ s \in S : \text{true} \} \). If it is false it denotes the empty set: \( \{ s \in S : \text{false} \} \). In the latter case there exists no program state in which \( x:=10; \) may be started and executed successfully.

**Exmp 2:** a second example is the assignment \( x:=x+1; \). Its effect can be characterized by:

\( \{ x=Kx \land x, x+1 \in \text{VS}(x) \} \ x:=x+1; \) \( \{ x=Kx+1 \land x \in \text{VS}(x) \} \)

If we assume \( \text{VS}(x) = 1..100 \) we see more directly the sets of states characterized by the precondition and by the postcondition:

\( \{ x=Kx \land 1 \leq x, x+1 \leq 100 \} \ x:=x+1; \)

\( \{ x=Kx+1 \land 1 \leq x \leq 100 \} \)

which may be transformed into:

\( \{ 1 \leq x \leq 99 \land x=Kx \} \ x:=x+1; \)

\( \{ 2 \leq x \leq 100 \land x=Kx+1 \} \)

In this case there are several states, in which \( x:=x+1; \) may be successfully executed: \( 1 \leq x \leq 99 \). If \( x=100 \) then an overflow will occur. The detailed effect of \( x:=x+1; \) is described using the specification variable \( Kx \) which expresses the relation...
between \( x \) before and after the execution of \( x := x + 1; \).

**Exmp 3:** a third example is a conditional statement which computes for certain values of \( x \) the absolute value of \( x \).

Let \( \text{VS}(x) = -128 .. +127 \).

\[
\{ x = -13 \}
\]

\[
\text{IF } x < 0 \text{ THEN } x := -x; \text{ FI}
\]

\[
\{ x = | -13 | = 13 \}
\]

A more detailed annotation shows that the statement really computes the absolute value of the initial value of \( x \):

\[
\{ x = -13 \}
\]

\[
\text{IF } x < 0 \text{ THEN}
\]

\[
\{ x = -13 \land -128 \leq -13 \leq 127 \}
\]

\[
x := -x;
\]

\[
\{ -x = -13 \land -128 \leq 13 \leq 127 \}
\]

\[
\text{FI}
\]

\[
\{ x = | -13 | = 13 \}
\]

Further simplification yields:

\[
\{ x = -13 \}
\]

\[
\text{IF } x < 0 \text{ THEN}
\]

\[
\{ x = -13 \land x := -x; \{ -x = -13 \}
\]

\[
\text{FI}
\]

\[
\{ x = | -13 | = 13 \}
\]

In this case we have only looked at a single starting state for the program \((x = -13)\). In section 4 we will do a more thorough analysis of this statement.

### 3 The wp-Calculus

In section 2 we have seen some examples of the precise characterization of the effect of statements. The treatment was somewhat ad hoc and we left it to the reader to be convinced of the correctness of the annotated program fragments. A more systematic treatment is possible if we define the relation between the precondition and the postcondition of a statement in a precise way. One possibility for this is the wp-calculus which computes for a given pair (statement, postcondition) the weakest i.e. most general precondition \(\text{wp}(\text{statement}, \text{postcondition})\) such that (1) the statement is successfully executable in any state of the \(\text{wp}(\text{statement}, \text{postcondition})\), and (2) the state after the execution of statement is in postcondition [Dij 76; DS 90]. If we express it in the language of states \(\text{wp}(\text{statement}, \text{post})\) is the largest set of states such that (1) the statement is successfully executable in any state of \(\text{wp}(\text{statement}, \text{post})\), and (2) the state after the execution of statement is in post [Win 96].

The effect of an assignment to a simple variable is defined by:

\[
\text{wp}("x:=\text{expr};", \text{postcond}) \equiv \text{def}(\text{expr}) \land \text{postcond}^x_{\text{expr}}
\]

This means that (1) if \(\text{expr}\) is evaluated before the execution of the assignment it must be well defined and its value must be in \(\text{VS}(x)\), and (2) whatever holds for the value of \(x\) after the execution holds for the value of \(\text{expr}\) before the execution.

**Exmp 4:** (let \(\text{VS}(x) = 1..100\))

\[
\text{wp}("x:=x+2;", x > 50) \equiv
\]

\[
1 \leq x+2 \leq 100 \land [x > 50]_{x+2} \equiv
\]

\[
-1 \leq x \leq 98 \land x+2 > 50 \equiv
\]

\[
49 \leq x \leq 98
\]

If the expression on the right hand side is more complicated the rule for \(\text{def}(\text{expr})\) must also express appropriate constraints for the subexpressions.

The effect of an IF-statement is defined by:

\[
\text{wp}("\text{IF } \text{be } \text{THEN } \text{stat1 ELSE } \text{stat2 FI}, \text{ poc}) \equiv
\]

\[
\text{def}(\text{be}) \land [\text{be } \land \text{wp}(\text{stat1}, \text{ poc}) \lor \neg \text{be } \land \text{wp}(\text{stat2}, \text{ poc})]
\]

This rule expresses the following:

a) the expression \(\text{be}\) must be welldefined in the state before execution of the IF-statement

b) the evaluation of \(\text{be}\) does not change the program state

c) if the value of \(\text{be}\) is true then \(\text{stat1}\) is executed

d) if the value of \(\text{be}\) is false then \(\text{stat2}\) is executed

This is what we expect to hold for the IF-statement.

**Exmp 5:** we want to show that the following IF-statement computes the absolute value of the initial value of \(x\) (let \(\text{VS}(x) = -128 .. 127\)):

\[
\{ -128 \leq x \leq 127 \land x = \text{K}x \}
\]

\[
\text{IF } x < 0 \text{ THEN } x := -x; \text{ ELSE null; FI}
\]

\[
\{ -128 \leq x \leq 127 \land x = |\text{K}x| \}
\]

\[
\text{wp}("\text{IF } x < 0 \text{ THEN } x := -x; \text{ ELSE null; FI}, x = |\text{K}x|) \equiv
\]

\[
\text{def}(x < 0) \land [x < 0 \land \text{wp}("x := -x;", x = |\text{K}x|) \lor x \geq 0 \land \text{wp}("\text{null;}", x = |\text{K}x|)] \equiv
\]
-128 ≤ x ≤ 127 ∧ 
[x<0 ∧ -128 ≤ x ≤ 127 ∧ x=|Kx| ∨ 
x ≥ 0 ∧ x=|Kx|] ⊨

-128 ≤ x ≤ 127 ∧ 
[-127 ≤ x ≤ -1 ∧ x=|Kx| ∨ 
0 ≤ x ≤ 127 ∧ x=|Kx|] ⊨

-127 ≤ x ≤ 127

We see immediately that the IF-statement does not work for x=-128 because the weakest precondition does not hold in this state:

-127 ≤ -128 ≤ 127 ⊨ false

4 The Frege Program Prover

It is quite tedious and error prone to perform the calculations of the wp-calculus by hand. This is a typical task for the computer. The Frege Program Prover (FPP) is a tool to perform such calculations. FPP can essentially do two things:

a) Compute the weakest precondition: wp(PF, Post). Compute the weakest precondition for a given program (fragment) PF and a given postcondition Post.

Example: wp(“v:=v+1;”, v>4)
⊗ v+1 ∈ VS(v) ∧ v+1 > 4
⊗ v+1 ∈ VS(v) ∧ v ≥ 4.

b) Check the correctness of a program (fragment): i.e. check whether a given program (fragment) PF satisfies a given specification (Pre,Post). This is usually expressed as a Hoare triple {Pre} PF {Post}. If PF satisfies the specification the triple is called consistent. This consistency is defined as: Pre ⇒ wp(PF,Post).

Example: { v>0 } v:=v+1; { v>4 }
⊗ v>0 ⇒ wp(“v:=v+1;”, v>4)
⊗ v>0 ⇒ v+1 ∈ VS(v) ∧ v ≥ 4
⊗ False.

The ATP tries to prove the VCs which are formally theorems in a first order predicate logic. Theorem proving is not as straightforward as the generation of the VCs. Therefore, the ATP is the hard part of program proving. Since we are not working in automatic theorem proving FPP uses a theorem prover from another party: Analytica [CZ 92] with some modifications and extensions implemented by S. Kauer. Due to the difficulty of automatic theorem proving the user of FPP may encounter a situation in which FPP cannot prove a certain VC, runs out of memory during proving or runs for a very long time. Such behavior is not completely different from that of a human theorem prover who may also not be able to prove a certain theorem. The capabilities of FPP just reflect the capabilities of the built-in ATP.

If we apply the FPP to the examples given earlier in the paper we obtain:

Exmp 1: Input to FPP:

--!Pre: -128 <= x and x < 127;
x := 10;
--!Post: x = 10;

Answer of FPP:

1) --!pre:-128 <= x AND 127 >= 1 + x
2) --! wp: True
3) --! wc: True
4) --! Result: proved
5) x := 10;
6) --!post: x = 10

The answer of FPP consists of the original input (lines 1, 5, and 6) and the result of the attempt to prove that the triple

{ -128 ≤ x ≤ 127 } x := 10; { x = 10 }

is consistent. As mentioned above the corresponding VC is

VC ⊨ -128 ≤ x ≤ 127 ⇒ wp(“x:=10;”, x=10)
FPP reports the weakest precondition in line 2 and the VC in line 3. In line 4 FPP says whether it could prove the VC. Since the VC is already true the proof is in this case a very simple one and has been successfully performed by FPP. That VC $\equiv$ true can be seen as follows: $wp("x:=10;", x=10) \equiv 10 = 10 \equiv$ true (FPP does in this step not take into account $VS(x)$). With this we obtain:

$$VC \equiv -128 \leq x \leq 127 \Rightarrow true \equiv true.$$  

**Exmp 3:** in this example we want to use FPP to compute for which values of $x$ the IF-statement computes the absolute value of $x$. We do this in two steps: (1) compute the weakest precondition; this gives us the set of values of $x$ for which the IF-statement can be successfully executed; (2) check whether the IF-statement computes the absolute value of $x$ for the values determined in step (1).

**Step 1:**  
*Input to FPP:*

```
IF x < 0 THEN x := -x; END IF;
--!Post: 0 <= x and x <= 127;
```

*Answer of FPP:*

```
--> wp:  ( 0 >= 1 + x AND 0 <= -x AND
--> wp:    -x <= 127
--> wp: OR 0 <= x AND x <= 127)
IF x < 0 THEN
  x := -x;
END IF;
--!post: (0 <= x AND x <= 127)
```

The somewhat clumsy expression for wp can be simplified to:

$$-127 \leq x \leq 127.$$  

**Step 2:**  
*Input to FPP:*

```
--!Pre: -127 <= x and x <= 127
--!Pre: and x = kx;
IF x < 0 THEN x := -x; END IF;
--!Post: 0 <= x and x <= 127
--!Post: and ((x=kx and kx >= 0)
--!Post: or (x = -kx and kx<0));
```

*Answer of FPP (simplified):*

```
--!pre: -127 <= x AND x <= 127 AND x=kx
--wp: -127 <= x AND x <= 127 AND x=-kx
--> OR -127 <= x AND x <= 127 AND x=kx
--> vc: -127 <= x AND x <= 127 AND x = kx
--> =>
---> -127 <= x AND x <= 127 AND x=-kx
--> OR -127 <= x AND x <= 127 AND x=kx
--> Result: proved
IF x < 0 THEN
  x := -x;
END IF;
--!post: (0 <= x) AND (x <= 127) AND
---> (x = kx AND kx >= 0 OR
---> x = -kx AND 0 > kx)
```

We see that the IF-statement computes the absolute value of $x$.

The next two examples are somewhat more complex than the previous ones. Both consist essentially of a loop, whereas the earlier examples are all purely linear.

For loops the computation of the weakest precondition is not as straightforward as for assignment, for IF or for CASE [Win 98]. In some cases it is possible to compute the weakest precondition of a WHILE-loop mechanically [Kau 99] but these new techniques have not yet been incorporated into FPP. FPP currently uses the traditional rule for loops as e.g. given in [Gri 83].

For a WHILE-loop we have to give a precondition, a postcondition, an invariant and a termination function. This is done according to the following scheme:

```
--!pre:  Precondition;
--!inv:  Invariant;
--!term: Termination function;
WHILE .... LOOP .... END LOOP;
```

Pre and Post are the specification of the problem, whereas Inv and Term are needed for verification purposes.

**Exmp6:** Computing the floor of the square root of a nonnegative integer number $n$.

The specification of this algorithm is as follows:

*Pre:* $n$ is nonnegative and the result variable $a$ has the initial value 0.

*Post:* $a$ has the desired value and $n$ has still the same value as in the precondition
Input to FPP:

```ada
--!Pre:  a=0 and n>=0 and n=Kn ;
--!Inv:  a**2<=n and n=Kn;
--!Term: n-a;
WHILE (a+1)**2 <= n LOOP
    a := a+1;
END LOOP;
```

FPP is able to prove the consistency of the annotated program given in the input. Therefore, the output of FPP could look like:

Output of FPP (shortened):

```
FPP (Frege Program Prover) University of Jena, Germany
The answer to your query is:
--!pre       : (a = 0 AND n >= 0 AND n = kn)
--!post      : ((1 + a)**2 >= 1 + n AND n >= a**2 AND n = kn)
--!inv       : (a**2 <= n AND n = kn)
--!term      : (-a + n)
--> Result    : proved
WHILE (a + 1) ** 2 <= n LOOP
    a := a + 1;
END LOOP;
```

In the output of FPP the input is repeated and lines produced by FPP begin with “--->”, i.e. these lines are also comment lines. Therefore, the output of FPP is still a legal Ada program (fragment).

Currently, FPP also displays the VCs which have to be proved in order to show the consistency of an annotated loop, i.e. the complete output looks like this:

Output of FPP:

```
FPP (Frege Program Prover) University of Jena, Germany
The answer to your query is:
--!pre       : (a = 0 AND n >= 0 AND n = kn)
--!post      : ((1 + a)**2 >= 1 + n AND n >= a**2 AND n = kn)
--!inv       : (a**2 <= n AND n = kn)
--!term      : (-a + n)
-->functionality -------------------------------------------------------
-->initial   :(a = 0 AND n >= 0 AND n = kn ==> a**2 <= n AND n = kn)
--> Result    : proved
-->induction :     ((1 + a)**2 <= n AND a**2 <= n AND n = kn)
-->     ==> ((1 + a)**2 <= n AND n = kn)
--> Result    : proved
-->final     :     ((1 + a)**2 >= 1 + n AND a**2 <= n AND n = kn)
-->     ==> ((1 + a)**2 >= 1 + n AND n = kn)
--> Result    : proved
-->termination ---------------------------------------------------------
-->initial   :((1 + a)**2 <= n AND a**2 <= n AND n = kn ==> -a + n >= 1)
--> Result    : proved
-->induction :((1 + a)**2 <= n AND a**2 <= n AND n = kn ==> -a + n >= -a + n)
--> Result    : proved
WHILE (a + 1) ** 2 <= n LOOP
    a := a + 1;
END LOOP;
```

The proof of consistency is done in five steps, three for the functionality and two for the termination of the loop. FPP lists the five VCs separately and indicates for each of them whether it has been proved. In this example all five VCs have been proved and therefore, the annotated loop is consistent.
Exmp7:  Linear searching an array for the index of a specific value.

This example is the implementation of the linear search in a one-dimensional array for the index of the first occurrence of a certain value.

The specification is as follows:
Pre: the array b contains at least one element and at least one element of b has the value we are looking for (which is the value of x).
Post: the value of ind is the index of the first occurrence of the value of x in b.

It is easy to see that neither x nor b are modified and therefore, this fact is not expressed in the assertions. Furthermore, it is assumed that b’ Range = 1..len.

Input to FPP:

```
--!pre   : ind=1 and len>=1 and (exists j: 1<=j and j<=len: b(j) = x);
--!post  : 1<=ind and ind<=len and b(ind) = x and
--!post  : not((exists j: 1<=j and j<=ind-1: b(j) = x));
--!inv   : 1<=ind and ind <=len and not ((exists j:1<=j and j<=len-1: b(j) = x))
--!inv   : and (exists j:1<=j and j<=len: b(j) = x);
--!term  : len+1-ind;
WHILE b(ind) /= x LOOP
  ind := ind+1;
END LOOP;
```

Output of FPP:

```
The answer to your query is:
--!pre       :     (ind = 1) AND (len >= 1)
--!pre       : AND ((exists j: 1 <= j AND j <= len AND b(j) = x))
--!post      :     (1 <= ind) AND (ind <= len) AND (b(ind) = x)
--!post      : AND (not(exists j: 1 <= j AND j <= -1 + ind AND b(j) = x))
--!inv       :      (1 <= ind) AND (ind <= len)
--!inv       : AND (not(exists j: 1 <= j AND j <= -1 + ind AND b(j) = x))
--!inv       : AND ((exists j: 1 <= j AND j <= len AND b(j) = x))
--!term      : (1 - ind + len)
-->functionality -------------------------------------------------------------
-->initial   :          (ind = 1) AND (len >= 1)
-->                 AND ((exists j: 1 <= j AND j <= len AND b(j) = x))
-->            ==>      (1 <= ind) AND (ind <= len)
-->                 AND (not(exists j: 1 <= j AND j <= -1 + ind AND b(j) = x))
-->                 AND ((exists j: 1 <= j AND j <= len AND b(j) = x))
--> Result    : proved
-->induction :          (b(ind) /= x) AND (1 <= ind) AND (ind <= len)
-->                 AND ((exists j: 1 <= j AND j <= len AND b(j) = x))
-->                 AND (not(exists j: 1 <= j AND j <= -1 + ind AND b(j) = x))
-->                 AND ((exists j: 1 <= j AND j <= len AND b(j) = x))
-->            ==>      (1 <= 1 + ind) AND (1 + ind <= len)
-->                 AND (not(exists j: 1 <= j AND j <= len AND b(j) = x))
-->                 AND ((exists j: 1 <= j AND j <= len AND b(j) = x))
--> Result    : proved
-->final     :          (b(ind) = x) AND (1 <= ind) AND (ind <= len)
-->                 AND ((exists j: 1 <= j AND j <= len AND b(j) = x))
-->                 AND (not(exists j: 1 <= j AND j <= -1 + ind AND b(j) = x))
-->                 AND ((exists j: 1 <= j AND j <= len AND b(j) = x))
-->            ==>      (1 <= ind) AND (ind <= len) AND (b(ind) = x)
-->                 AND (not(exists j: 1 <= j AND j <= -1 + ind AND b(j) = x))
-->                 AND ((exists j: 1 <= j AND j <= len AND b(j) = x))
--> Result    : proved
-->termination ----------------------------------------------------------------
-->initial   :          (b(ind) /= x) AND (1 <= ind) AND (ind <= len)
-->                 AND ((exists j: 1 <= j AND j <= len AND b(j) = x))
-->                 AND (not(exists j: 1 <= j AND j <= -1 + ind AND b(j) = x))
-->                 AND ((exists j: 1 <= j AND j <= len AND b(j) = x))
-->            ==>      (1 - ind + len >= 1)
--> Result    : proved
-->induction :          (b(ind) /= x) AND (1 <= ind) AND (ind <= len)
```
5 Conclusions

If software engineers want to design programs as other engineers are designing their artifacts a framework for the quantitative analysis of programs is necessary. There exist several calculi to define the effect of a program in a quantitative manner: e.g. the wp-calculus or the relational calculus of Hehner [Heh 93]. As for other calculations in engineering it is very useful to let the computer do these calculations. In other branches of engineering the calculations necessary are typically numerical ones. For these a lot of tools are available. For the calculations necessary to compute the effect of programs no tools are readily available.

In this paper we have described the Frege Program Prover, an experimental tool which supports the SW engineer in program analysis.

Acknowledgments

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References


